## C. U. SHAH UNIVERSITY Winter Examination-2022

## **Subject Name : Classical Mechanics**

| Subject Code : 5SC0 | 1CLM1            | Branch: M.Sc. (Physics) |           |  |
|---------------------|------------------|-------------------------|-----------|--|
| Semester: 1         | Date: 03/01/2023 | Time: 11:00 To 02:00    | Marks: 70 |  |

## **Instructions:**

- (1) Use of Programmable calculator and any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

## **SECTION – I**

| Q-1 |    | Attempt the Following questions.  | (07) |
|-----|----|---|------|
|     | a. | Define Generalized Coordinates.   | 01   |
|     | b. | Define Constraints.   | 01   |
|     | c. | Write Hamilton's equation of motion.  | 01   |
|     | d. | Write the general expression for Euler-Lagrange equation of motion.                 | 01   |
|     | e. | Define Degree of Freedom.   | 01   |
|     | f. | State the conservation of angular momentum.   | 01   |
|     | g. | State the main difference between Newtonian and Lagrangian for system of particles. | 01   |
| Q-2 |    | Attempt all questions.  | (14) |
| -   | Α  | Write a note on Generalized coordinates.  | 07   |
|     | B  | Obtain the Lagrangian for a simple Atwood's machine.                                | 07   |
|     |    | OR  |      |
| Q-2 |    | Attempt all questions.  | (14) |
|     | Α  | Using Hamilton's Equation, solve the Oscillator problem.                            | 07   |
|     | B  | Explain in detail the Degree of freedom with examples.                              | 07   |
| Q-3 |    | Attempt all questions.  | (14) |
| -   | Α  | Derive the Euler-Lagrange's equation of motion.                                     | 07   |
|     | B  | Explain in detail various types of constraints with suitable examples.              | 07   |
|     |    | OR  |      |
| Q-3 |    | Attempt all questions.  |      |
|     | Α  | Deduce the expression for D'Alembert's Principle.                                   | 07   |
|     | B  | Derive the equation of Hamilton's principle equation.                               | 07   |
|     |    | SECTION – II  |      |
| Q-4 |    | Attempt the Following questions.  | (07) |

|    | Attempt the ronowing questions.                                  | ( <b>0</b> )       |
|----|--|--------------------|
| a. | Give the expression for Hamilton's canonical equation of motion. | 01                 |
| b. | Define Stable Equilibrium.                                       | 01                 |
|    |  | Page <b>1</b> of 2 |



| c. | c. State two significances of Hamilton over Lagrangian.                                       |   |
|----|---|---|
| d  | Why Hamilton Principle is also known as 'Variational Principle'?                              | 01  |
| e. | What do you mean by invariance under canonical transformation?                                | 01  |
| f. | Give some examples where small oscillation theory is applicable.                              | 01  |
| g. | Define normal modes.  | 01  |
|    | Attempt all questions.  | (14)  |
| Α  | Explain Poisson's theorem in detail.  | 07  |
| B  | Using the explanation of Canonical Transformation, obtain the Hamilton's canonical equations. | 07  |
|    | OR  |   |
|    | Attempt all questions.  |   |
| Α  | Explain in detail Generating function.  | 07  |
| B  | Deduce the characteristic equation for the case of two coupled oscillators.                   | 07  |
|    | Attempt all questions.  | (14)  |
| Α  | Enumerate on Poisson Bracket.   | 07  |
| B  | Explain the working of Generating functions in obtaining new Hamiltonian                      | 07  |
|    | for a system.   |   |
|    | OR  |   |
|    | Attempt all questions.  |   |
| Α  | Explain the Hamilton-Jacobi theory.   | 07  |
|    | c.<br>d.<br>e.<br>f.<br>g.<br>A<br>B<br>A<br>B<br>A<br>B<br>A<br>B                            | <ul> <li>c. State two significances of Hamilton over Lagrangian.</li> <li>d. Why Hamilton Principle is also known as 'Variational Principle'?</li> <li>e. What do you mean by invariance under canonical transformation?</li> <li>f. Give some examples where small oscillation theory is applicable.</li> <li>g. Define normal modes.</li> <li>Attempt all questions.</li> <li>A Explain Poisson's theorem in detail.</li> <li>B Using the explanation of Canonical Transformation, obtain the Hamilton's canonical equations.</li> <li>Attempt all questions.</li> <li>A Explain in detail Generating function.</li> <li>B Deduce the characteristic equation for the case of two coupled oscillators.</li> <li>Attempt all questions.</li> <li>A Enumerate on Poisson Bracket.</li> <li>B Explain the working of Generating functions in obtaining new Hamiltonian for a system.</li> <li>OR</li> <li>Attempt all questions.</li> <li>A Enumer all questions.</li> <li>A Enumerate on Poisson Bracket.</li> <li>B Explain the Hamilton-Jacobi theory.</li> </ul> |

**B** Comment on Kepler's Problem using Lagrangian formulation. **07** 

